Infrared signatures of the spin-Peierls transition in CuGeO$_3$

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We investigated the infrared reflectivity of several Mg- and Si-substituted CuGeO$_3$ single crystals. The temperature-dependent $b$-axis and $c$-axis optical response is reported. For $T<T_{\text{SP}}$ we detected the activation of zone-boundary phonons along the $b$ axis of the crystal on the pure sample and for 1% Mg and 0.7% Si concentrations. From a detailed analysis of the phonon parameters the redshift of the $B_{2g}$ mode at 48 cm$^{-1}$ is observed and discussed in relation to the soft mode expected to drive the spin-Peierls phase transition in CuGeO$_3$. Moreover, the polarization dependence of a magnetic excitation measured in transmission at 44 cm$^{-1}$ has been investigated. [S0163-1829(97)51942-4]

In 1993, CuGeO$_3$ was recognized, on the basis of magnetic susceptibility measurements,\textsuperscript{3} as an inorganic compound showing a spin-Peierls (SP) transition. This transition consists of the lattice distortion (due to the magnetoelastic coupling between the one-dimensional spin system and the three-dimensional phonon system) that occurs together with the formation of a spin-singlet ground state and the opening of a finite energy gap in the magnetic excitation spectrum. This discovery has renewed the interest in the field of the SP phenomenon by a very broad variety of experimental techniques. Furthermore, CuGeO$_3$ seems to be a good candidate for the observation of a soft mode in the phonon spectrum, upon passing through the SP transition. In fact, a well-defined soft mode is expected in those theoretical models describing an SP system in terms of a linear coupling between lattice and magnetic degrees of freedom.\textsuperscript{3,4} During the last few years both the structural deformation and the spin gap have been characterized in detail by x-ray and neutron-scattering experiments.\textsuperscript{5-9} So far no soft mode has yet been detected in CuGeO$_3$.

In this paper we present a detailed spectroscopic study of the vibrational and electronic signatures of the SP transition in pure and doped CuGeO$_3$. We concentrate on the nature of the transition and on the dynamical interplay between spins and phonons.

We investigated the far- and mid-infrared reflectivity (20–6000 cm$^{-1}$) of several Cu$_{1-x}$Mg$_x$GeO$_3$ ($x=0.0,0.01$) and CuGe$_{1-x}$Si$_x$O$_3$ ($x=0.007,0.05,0.1$) single crystals. These high-quality single crystals were grown from the melt by a floating zone technique.\textsuperscript{10} Samples with dimensions of approximately $1\times3\times6$ mm$^3$ were aligned by conventional Laue diffraction and mounted in a liquid He flow cryostat to study the temperature dependence of the optical properties between 4 and 300 K. The reflectivity measurements were performed with a Fourier transform spectrometer (Bruker IFS 113v), operating in near normal incidence configuration with polarized light in order to probe the optical response of the crystals along the $b$ and the $c$ axes. The absolute reflectivities were obtained by calibrating the data acquired on the samples against a gold mirror.

The number and the symmetry of the infrared active phonons expected for the high-temperature undistorted phase and the low-temperature SP phase of CuGeO$_3$ can be obtained from a group theoretical analysis of the lattice vibrational modes. At room temperature CuGeO$_3$ has an orthorhombic crystal structure with lattice parameters $a=4.81$, $b=8.47$, and $c=2.941$ Å and space group $Pbmm$ or, equivalently, $Pmmn$ in standard setting.\textsuperscript{11} The building blocks of the structure are edge-sharing CuO$_6$ octahedra and corner-sharing GeO$_4$ tetrahedra stacked along the $c$ axis of the crystal and resulting in Cu$^{2+}$ and Ge$^{4+}$ chains parallel to the $c$ axis. These chains are linked together via the O atoms [denoted as O(2)] and form layers parallel to the $b$-$c$ plane weakly coupled along the $a$ axis. The irreducible representation of the optical vibrations of CuGeO$_3$, in setting $Pbmm$, for $T>T_{\text{SP}}$ is\textsuperscript{12}

$$\Gamma=4A_g(aa,bb,cc)+4B_{1g}(ab)+3B_{2g}(ac)+B_{3g}(bc)$$
$$+3B_{1u}(E||c)+5B_{2u}(E||b)+5B_{3u}(E||a),$$

Corresponding to an expectation of 12 Raman active modes ($4A_g+b4B_{1g}+3B_{2g}+B_{3g}$) and 13 infrared active modes ($3B_{1u}+5B_{2u}+5B_{3u}$). Below $T_{\text{SP}}$ the crystal structure is still orthorhombic, but with lattice parameters $a'=2\times a$, $b'=b$, and $c'=2\times c$ and space group $Bbcm$ or, equivalently, $Cmca$ in standard setting.\textsuperscript{5,7} The distortion of the lattice in the phase transition can be characterized as the dimerization of the Cu-Cu pairs along the $c$ axis (dimerization out of phase in neighboring chains), together with the rotation of the GeO$_4$ tetrahedra around the axis defined by the O(1) sites (rotation opposite in sense for neighboring tetrahedra).
Moreover, the O(2) sites of the undistorted structure split in an equal number of O(2a) and O(2b) sites, distinguished by the distances O(2a)-O(2a) and O(2b)-O(2b) shorter and larger than O(2)-O(2), respectively. The irreducible representation of the optical vibrations, in setting $Bbcm$, for $T < T_{\text{SP}}$ is:

$$\Gamma_{\text{SP}} = 8A_g(aa, bb, cc) + 9B_{1g}(ab) + 7B_{2g}(ac) + 6B_{3g}(bc) + 5B_{1u}(E || c) + 9B_{2u}(E || b) + 8B_{3u}(E || a).$$

Therefore 30 Raman active modes ($8A_g + 9B_{1g} + 7B_{2g} + 6B_{3g}$) and 22 infrared active modes ($5B_{1u} + 9B_{2u} + 8B_{3u}$) are expected for CuGeO$_3$ in the SP phase, all the additional vibrations being zone-boundary modes activated by the folding of the Brillouin zone. In particular, the number of infrared active phonons is expected to increase from 5 to 8, 5 to 9, and 3 to 5 for light polarized along the $a$, $b$, and $c$ axis, respectively, upon passing through the phase transition.

The $c$- and $b$-axis reflectivity spectra of pure CuGeO$_3$ are plotted in Fig. 1, for $T = 15$ K (circles) and $T = 4$ K (solid line). The data, characteristic of an ionic insulating material, are shown up to 1000 cm$^{-1}$ which covers the full phonon spectrum. For $T > T_{\text{SP}}$ three phonons are detected along the $c$ axis ($\omega_{TO} \approx 167$, 528, and 715 cm$^{-1}$ for $T = 15$ K), and five along the $b$ axis ($\omega_{TO} \approx 48, 210, 286, 376$, and 766 cm$^{-1}$ for $T = 15$ K), in agreement with the theoretical expectation. The structure in Fig. 1(a) between 200 and 400 cm$^{-1}$ is due to a leakage of the modes polarized along the $c$ axis. The feature at approximately 630 cm$^{-1}$ in Fig. 1(b) is a leakage of a mode polarized along the $a$ axis. Whereas for $E||c$, the spectra are exactly identical, a new feature is detected in the SP phase at 800 cm$^{-1}$ for $E||b$, as shown in the inset of Fig. 1(b). A careful investigation of temperatures ranging from 4 to 15 K (see Fig. 2) clearly shows that this feature, that falls in the frequency region of high reflectivity for the $B_{2u}$ phonon at 766 cm$^{-1}$ and therefore shows up in reflectivity mainly for its absorption, is activated by the SP transition. It corresponds to a new absorption peak in conductivity, superimposed on a background due to the Lorentzian tail of the close $B_{3u}$ mode (see inset of Fig. 2). We observed the same peak (at the same resonant frequency) also on 1% Mg and 0.7% Si-doped single crystals, but not on 5 and 10% Si-doped samples, where we did not find any sign of the SP transition also on the basis of magnetic susceptibility measurements.

By fitting the reflectivity spectra with Lorentz oscillators for the optical phonons it is possible to obtain the temperature dependence of the oscillator strength for the 800 cm$^{-1}$ feature. The results are plotted in Fig. 3, together with the peak intensity of the superlattice reflection measured by Harris$ et al.$ in an x-ray scattering experiment on a pure CuGeO$_3$ single crystal characterized, as our sample, by $T_{\text{SP}} \approx 13.2$ K. From the perfect agreement of the infrared and x-ray scattering results on pure CuGeO$_3$ and from the observation that the resonant frequency is not shifting at all with temperature, we can conclude that the peak at 800 cm$^{-1}$ corresponds to a pure lattice excitation and the oscillator strength is proportional to the symmetry-breaking displacement of the atoms squared. The same conclusions can be obtained for the 1% Mg- and 0.7% Si-doped samples, where $T_{\text{SP}}$ of approximately 12.4 and 9.3 K, respectively, are observed (in these two cases the data can be compared, for 0.7% Si doping, to those presented in Ref. 15 and, for 1% Mg doping, to those reported in Ref. 16 for a 0.9% Zn-doped sample, because no x-ray or neutron-scattering data are available in the literature for Mg-doped CuGeO$_3$). Moreover, as this activated line does not show any frequency shift as a function of Si and Mg doping, we can conclude that it
has to be a folded zone-boundary mode related to the $B_{2u}$ phonon observed at 766 cm$^{-1}$, which is mainly an oxygen vibration. This gives for the $B_{2u}$ mode an energy dispersion, over the full Brillouin zone, of the order of 34 cm$^{-1}$ = 4.22 meV at $T = 15$ K.

The reasons for not observing in our reflectivity spectra for $T < T_{SP}$ all the phonons predicted from the group theoretical analysis, are probably the small values of the atomic displacements involved in the SP transition (with a correspondingly small oscillator strength of zone-boundary modes), and/or possibly the small dispersion of the optical branches of some of the lattice vibrations. However, it is not surprising that the only activated mode has been detected along the $b$ axis of the crystal. In fact, it is for this axis that for $T < T_{SP}$ a spontaneous thermal contraction has been observed, which can be responsible for a relative increase of the oscillator strength of the phonons polarized along the $b$ axis with respect to those polarized along the $c$ axis.

In Fig. 3 the results of a fit of the experimental data by the equation $(1 - T/T_{SP})^2$ over a broad temperature range are also plotted, for the pure sample. We obtained $\beta = 0.26 \pm 0.02$ in agreement with Ref. 17. However, the best fit value of $\beta$ is strongly dependent on the temperature range chosen to fit the data. If only points very close (within one Kelvin) to $T_{SP}$ are considered, the value $\beta = 0.36 \pm 0.03$ is obtained, as reported in Ref. 6. It is not possible to perform the same fit for the data acquired on doped samples because they are characterized by an upturned curvature near $T_{SP}$, which can be explained in terms of a distribution of transition temperatures due to the disorder introduced upon doping the system.

As far as the dynamical interplay between spins and phonons in CuGeO$_3$ is concerned, it is clear from the reflectivity spectra plotted in Fig. 1 that a well-defined soft mode, driving the structural deformation in CuGeO$_3$, has not been detected in our measurements. However, interesting information can be drawn from the temperature dependence of the phonon parameters obtained from the fit of the reflectivity data for the pure sample. In Fig. 4 the frequency shift (in percent) for the $B_{1u}$ modes ($E \parallel b$) and the $B_{2u}$ modes ($E \parallel b$) is plotted as a function of temperature. We can clearly observe that the $B_{2u}$ mode at 48 cm$^{-1}$ is the only one showing an evident monotonic redshift from 300 to 15 K. This can be understood in terms of the normal-mode displacements obtained by Popović et al. via a shell-model lattice dynamical calculation. In fact, this particular $B_{2u}$ mode, as well as the Raman active $B_{1g}$ at 116 cm$^{-1}$, consists mainly of the rotation (accompanied by a slight internal distortion) of the GeO$_4$ tetrahedra around the axis defined by the O(1) sites. It is precisely this "hinge motion" represented in terms of normal-mode displacements at $k = (\pi/a, 0, \pi/c)$ which, together with the dimerization of the Cu-Cu pairs along the $c$ axis, corresponds to the structural deformation involved in the SP phase transition. The $B_{2u}$ mode at 48 cm$^{-1}$ has approximately the same character. Below $T_{SP}$ this mode shows only a small blueshift. More noticeable there is a large ($\sim 15\%$) reduction of oscillator strength $S$ (see inset of Fig. 4). One may speculate at this point, that a full softening is also absent for the phonons at $k = (\pi/a, 0, \pi/c)$, implying that the phase transition is not driven by a softening of the phonon spectrum at $k = (\pi/a, 0, \pi/c)$, but by a change in electronic structure which in turn determines the dynamical charge of the ions and the interatomic force constants. In this scenario the large change in oscillator strength of some of the vibrational modes results from a change in ionicity, or, in other words, a transfer of spectral weight from the elastic degrees of freedom to electronic excitations.

A last remark has to be made regarding the temperature dependence of the $B_{2u}$ mode ($B_{3u}$ in standard setting) observed at 286 cm$^{-1}$. In a recent paper a softening of this phonon, upon going through the phase transition, was suggested. This is not confirmed by our results which show no considerable frequency shift for this resonance upon reducing the temperature from 15 to 4 K (see Fig. 4). On the other hand a reduction of both the scattering rate and the oscillator strength is observed, which can explain the double-peak structure in the reflectance ratio $R(20\text{ K})/R(5\text{ K})$ reported in Ref. 19.

Usually in optical spectroscopy direct singlet-triplet excitations are not detectable or very weak. However, such a transition has been observed at 44.3 cm$^{-1}$ in an infrared transmission experiment where the singlet-triplet nature of the transition was demonstrated by the Zeeman splitting ob-

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**FIG. 3.** Temperature dependence of the oscillator strength of the zone-boundary mode observed for $E \parallel b$ at 800 cm$^{-1}$ on pure (filled circles), 1% Mg-doped (triangles), and 0.7% Si-doped (diamonds) CuGeO$_3$ single crystals. For comparison the x-ray scattering data of Harris et al. (Ref. 14) are also plotted (open circles).

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**FIG. 4.** Temperature dependence of the frequency shift (in percent) of the transverse optical phonons observed for $E \parallel b$ and $E \parallel c$ on the pure single crystal of CuGeO$_3$. In the inset the oscillatory strength $S$ of the mode detected at 48 cm$^{-1}$, for $E \parallel b$, is plotted versus the temperature.
in magnetic field. In a very recent paper this line was interpreted as a magnetic excitation across the gap at the wave vector \( \mathbf{b} = (0, \pi/b, 0) \) in the Brillouin zone, activated by the existence of staggered magnetic fields along the \( b \) axis. In order to study this interpretation we measured the far-infrared transmission on the pure CuGeO\(_3\) single crystal for \( E\parallel b \) and \( E\parallel c \). The absorbance difference spectra are reported in Fig. 5, where they have been shifted for clarity. For \( E\parallel c \) no absorption is observed. However, for \( E\parallel b \) an absorption peak, showing the appropriate temperature dependence, is present at approximately 44 cm\(^{-1}\). One has to note that the feature at 48 cm\(^{-1}\) is produced by the low-energy \( B_{2u} \) phonon. In fact, due to the strong temperature dependence of its parameters, this line does not cancel out completely in the ratios of transmission spectra measured at different temperatures. The observed polarization dependence puts a strong experimental constraint on the possible microscopic mechanism giving rise to the singlet-triplet absorption peak.

In conclusion, we have investigated the temperature-dependent phonon spectrum of pure and doped CuGeO\(_3\), by means of infrared reflectivity measurements. We observed the activation of zone-boundary phonons along the \( b \) axis of the crystals, for \( T<T_{SP} \), and the redshift of the \( B_{2u} \) mode at 48 cm\(^{-1}\). The latter result has been discussed in relation to the role played by this lattice vibration in driving the system into the dimerized phase. Moreover, a magnetic excitation has been measured in transmission at 44 cm\(^{-1}\) and its polarization dependence investigated.

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