

Two gaps make a high-temperature superconductor?

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Abstract

One of the keys to the high-temperature superconductivity puzzle is the identification of the energy scales associated with the emergence of a coherent condensate of superconducting electron pairs. These might provide a measure of the pairing strength and of the coherence of the superfluid, and ultimately reveal the nature of the elusive pairing mechanism in the superconducting cuprates. To this end, a great deal of effort has been devoted to investigating the connection between the superconducting transition temperature T_c and the normal-state pseudogap crossover temperature T^* . Here we present a review of a large body of experimental data which suggests a coexisting two-gap scenario, i.e. superconducting gap and pseudogap, over the whole superconducting dome. We focus on spectroscopic data from cuprate systems characterized by $T_c^{\max} \sim 95$ K, such as $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$, $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ and $\text{HgBa}_2\text{CuO}_{4+\delta}$, with particular emphasis on the Bi-compound which has been the most extensively studied with single-particle spectroscopies.

(Some figures in this article are in colour only in the electronic version)

This article was invited by Professor L Greene.

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1. Introduction

Since their discovery [1], the copper-oxide high- T_c superconductors (HTSCs) have become one of the most investigated class of solids [2–24]. However, despite the intense theoretical and experimental scrutiny, an understanding of the mechanism that leads to superconductivity is still lacking. At the very basic level, what distinguishes the cuprates from the conventional superconductors is the fact that they are doped materials, the highly atomic-like Cu 3d orbitals give rise to strong electron correlations (e.g. the undoped parent compounds are antiferromagnetic Mott–Hubbard-like insulators), and the superconducting elements

are weakly-coupled two-dimensional layers (i.e. the celebrated square CuO_2 planes). Among the properties that are unique to this class of superconducting materials, in addition to the unprecedented high superconducting T_c , the normal-state gap or *pseudogap* is perhaps the most noteworthy. The pseudogap was first detected in the temperature dependence of the spin-lattice relaxation and Knight shift in nuclear magnetic resonance and magnetic susceptibility studies [25]. The Knight shift is proportional to the density of states at the Fermi energy; a gradual depletion was observed below a crossover temperature T^* , revealing the opening of the pseudogap well above T_c on the underdoped side of the HTSC phase diagram (figure 1). As the estimates based on thermodynamic

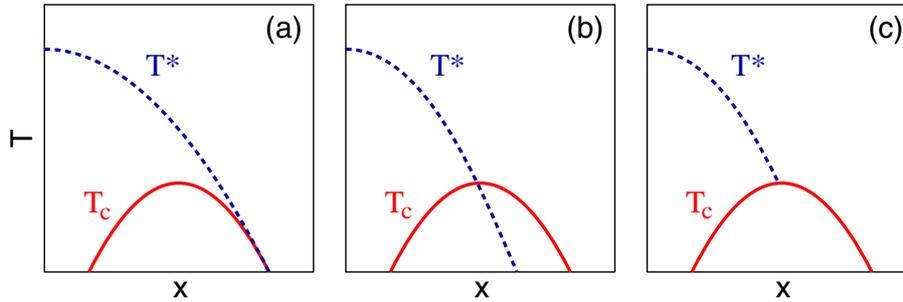


Figure 1. Various scenarios for the interplay of pseudogap (blue dashed line) and superconductivity (red solid line) in the temperature-doping phase diagram of the HTSCs. While in (a) the pseudogap merges gradually with the superconducting gap in the strongly overdoped region, in (b) and (c) the pseudogap lines intersect the superconducting dome at about optimal doping (i.e. maximum T_c). In most descriptions, the pseudogap line is identified with a crossover with a characteristic temperature T^* rather than a phase transition; while at all dopings $T^* > T_c$ in (a), beyond optimal doping $T^* < T_c$ in (b) and T^* does not even exist in (c). Adapted from [12].

quantities are less direct than in spectroscopy we, in the course of this review, concentrate mainly on spectroscopic results; more information on other techniques can be found in the literature [5].

As established by a number of spectroscopic probes, primarily angle-resolved photoemission spectroscopy, [26,27] the pseudogap manifests itself as a suppression of the normal-state electronic density of states at E_F exhibiting a momentum dependence reminiscent of a $d_{x^2-y^2}$ functional form. For hole-doped cuprates, it is largest at Fermi momenta close to the antinodal region in the Brillouin zone—i.e. around $(\pi, 0)$ —and vanishes along the nodal direction—i.e. the $(0, 0)$ to the (π, π) line. Note however that, strictly speaking, photoemission and tunneling probe a suppression of spectral weight in the single-particle spectral function, rather than directly of density of states; to address this distinction, which is fundamental in many-body systems and will not be further discussed here, it would be very interesting to investigate the quantitative correspondence between nuclear magnetic resonance and single-particle spectroscopy results. Also, no phase information is available for the pseudogap since, unlike the case of optimally and overdoped HTSCs [28], no phase-sensitive experiments have been reported for the underdoped regime where $T^* \gg T_c$.

As for the doping dependence, the pseudogap T^* is much larger than the superconducting T_c in underdoped samples, it smoothly decreases upon increasing the doping, and seems to merge with T_c in the overdoped regime, eventually disappearing together with superconductivity at doping levels larger than $x \sim 0.27$ [5–24].

In order to elaborate on the connection between pseudogap and high- T_c superconductivity, or in other words between the two energy scales E_{pg} and E_{sc} identified by T^* and T_c , respectively, let us start by recalling that in conventional superconductors the onset of superconductivity is accompanied by the opening of a gap at the chemical potential in the one-electron density of states. According to the Bardeen–Cooper–Schrieffer (BCS) theory of superconductivity [29], the gap energy provides a direct measure of the binding energy of the two electrons forming a Cooper pair (the two-particle bosonic entity that characterizes the superconducting state). It therefore came as a great surprise

that a gap, i.e. the pseudogap, was observed in the HTSCs not only in the superconducting state as expected from BCS, but also well above T_c . Because of these properties and the hope it might reveal the mechanism for high-temperature superconductivity, the pseudogap phenomenon has been very intensely investigated. However, no general consensus has been reached yet on its origin, its role in the onset of superconductivity itself, and not even on its evolution across the HTSC phase diagram.

As discussed in three recent papers on the subject [12, 15, 17], and here summarized in figure 1, three different phase diagrams are usually considered with respect to the pseudogap line. While Millis [15] opts for a diagram like the one in figure 1(a), Cho [17] prefers a situation where the pseudogap line meets the superconducting dome at $x \simeq 0.16$ (figures 1(b) and (c)); Norman *et al* [12] provide a comprehensive discussion of the three different possibilities. One can summarize some of the key questions surrounding the pseudogap phenomenon and its relevance to high-temperature superconductivity as follows [12, 15, 17]:

1. Which is the correct phase diagram with respect to the pseudogap line?
2. Does the pseudogap connect to the insulator quasiparticle spectrum?
3. Is the pseudogap the result of some one-particle band structure effect?
4. Or, alternatively, is it a signature of a two-particle pairing interaction?
5. Is there a true order parameter defining the existence of a pseudogap phase?
6. Do the pseudogap and a separate superconducting gap coexist below T_c ?
7. Is the pseudogap a necessary ingredient for high- T_c superconductivity?

In this review we revisit some of these questions, with specific emphasis on the one- versus two-gap debate. Recently, this latter aspect of the HTSCs has been discussed in great detail by Goss Levi [30], in particular based on scanning-tunneling microscopy data from various groups [31–33]. Here we expand this discussion to include the plethora of experimental results available from a wide variety of techniques. We

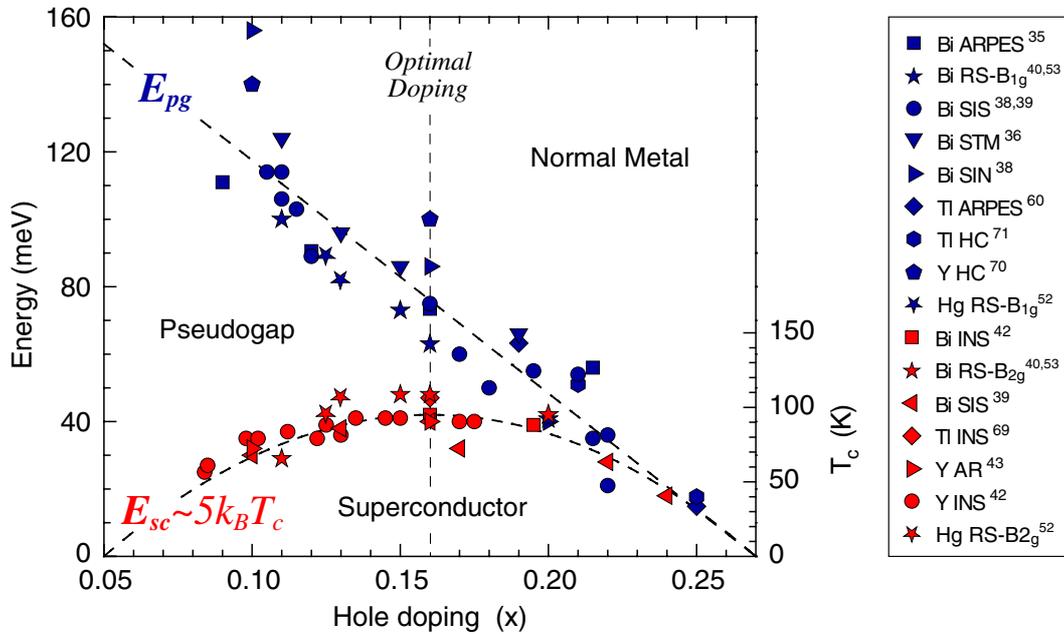


Figure 2. Pseudogap ($E_{pg} = 2\Delta_{pg}$) and superconducting ($E_{sc} \sim 5k_B T_c$) energy scales for a number of HTSCs with $T_c^{\max} \sim 95$ K (Bi2212, Y123, Tl2201 and Hg1201). The datapoints were obtained, as a function of hole doping x , by angle-resolved photoemission spectroscopy (ARPES), tunneling (STM, SIN, SIS), Andreev reflection (AR), Raman scattering (RS) and heat conductivity (HC). On the same plot we are also including the energy Ω_r of the magnetic resonance mode measured by inelastic neutron scattering (INS), which we identify with E_{sc} because of the striking quantitative correspondence as a function of T_c . The data fall on two universal curves given by $E_{pg} = E_{pg}^{\max}(0.27 - x)/0.22$ and $E_{sc} = E_{sc}^{\max}[1 - 82.6(0.16 - x)^2]$, with $E_{pg}^{\max} = E_{pg}(x = 0.05) = 152 \pm 8$ meV and $E_{sc}^{\max} = E_{sc}(x = 0.16) = 42 \pm 2$ meV (the statistical errors refer to the fit of the selected datapoints; however, the spread of all available data would be more appropriately described by ± 20 and ± 10 meV, respectively).

show that one fundamental and robust conclusion can be drawn: the HTSC phase diagram is dominated by two energy scales, the superconducting transition temperature T_c and the pseudogap crossover temperature T^* , which converge to the very same critical point at the end of the superconducting dome. Establishing whether this phenomenology can be conclusively described in terms of a coexisting two-gap scenario, and what the precise nature of the gaps would be, will require a more definite understanding of the quantities measured by the various probes.

2. Emerging phenomenology

The literature on the HTSC superconducting gap and/or pseudogap is very extensive and still growing. In this situation it seems interesting to go over the largest number of data obtained from as many experimental techniques as possible, and look for any possible systematic behavior that could be identified. This is the primary goal of this focused review. We want to emphasize right from the start that we are not aiming at providing exact quantitative estimates of superconducting and pseudogap energy scales for any specific compound or any given doping. Rather, we want to identify the general phenomenological picture emerging from the whole body of available experimental data [5, 9, 13, 16, 18, 34–72].

We consider some of the most direct probes of low-energy, electronic excitations and spectral gaps, such as angle-resolved photoemission (ARPES), scanning-tunneling microscopy (STM), superconductor/insulator/normal-metal

(SIN) and superconductor/insulator/superconductor (SIS) tunneling, Andreev reflection tunneling (AR) and Raman scattering (RS), as well as less conventional probes such as heat conductivity (HC) and inelastic neutron scattering (INS). The emphasis in this review is on spectroscopic data because of their more direct interpretative significance; however, these will be checked against thermodynamic/transport data whenever possible. With respect to the spectroscopic data, it is important to differentiate between single-particle probes such as ARPES and STM, which directly measure the one-electron excitation energy Δ with respect to the chemical potential (on both side of E_F in STM), and two-particle probes such as Raman and inelastic neutron scattering, which instead provide information on the particle-hole excitation energy 2Δ . Note that the values reported here are those for the ‘full gap’ 2Δ (associated with either E_{sc} or E_{pg}), while frequently only half the gap Δ is given for instance in the ARPES literature. In doing so one implicitly assumes that the chemical potential lies half-way between the lowest-energy single-electron removal and addition states; this might not necessarily be correct but appears to be supported by the direct comparison between ARPES and STM/Raman results. A more detailed discussion of the quantities measured by the different experiments and their interpretation is provided in the following subsections. Here we would like to point out that studies of B_{2g} and B_{1g} Raman intensity [19, 40, 52], heat conductivity of nodal quasiparticles [70, 71] and neutron magnetic resonance energy Ω_r [42] do show remarkable agreement with superconducting or pseudogap energy scales as inferred by single-particle

Table 1. Pseudogap E_{pg} and superconducting E_{sc} energy scales (2Δ) as inferred, for optimally doped Bi2212 ($T_c \sim 90\text{--}95$ K), from different techniques and experiments. Abbreviations are given in the main text, while the original references are listed.

Experiment	Energy	meV	References
ARPES— $(\pi, 0)$ peak	E_{pg}	80	[34, 35]
Tunneling—STM	„	70	[18, 36]
Tunneling—SIN	„	85	[37]
Tunneling—SIS	„	75	[38, 39]
Raman— B_{1g}	„	65	[40]
Electrodynamics	„	80	[5, 41]
Neutron— (π, π) Ω_r	E_{sc}	40	[42]
Raman— B_{2g}	„	45	[40]
Andreev	„	45	[43]
SIS—dip	„	40	[39]

probes, or with the doping dependence of T_c itself. Thus they provide, in our opinion, an additional estimate of E_{sc} and E_{pg} energy scales.

As for the choice of the specific compounds to include in our analysis, we decided to focus on those HTSCs exhibiting a similar value of the maximum superconducting transition temperature T_c^{\max} , as achieved at optimal doping, so that the data could be quantitatively compared without any rescaling. We have therefore selected $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ (Bi2212), $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ (Y123), $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ (Tl2201) and $\text{HgBa}_2\text{CuO}_{4+\delta}$ (Hg1201), which have been extensively investigated and are all characterized by $T_c^{\max} \sim 95$ K [73] (with particular emphasis on Bi2212, for which the most extensive set of single-particle spectroscopy data is available). It should also be noted that while Bi2212 and Y123 are ‘bilayer’ systems, i.e. their crystal structure contains as a key structural element sets of two adjacent CuO_2 layers, Tl2201 and Hg1201 are structurally simpler single CuO_2 -layer materials. Therefore, this choice of compounds ensures that our conclusions are generic to all HTSCs with a similar T_c , independent of the number of CuO_2 layers.

A compilation of experimental results for the magnitude of pseudogap ($E_{pg} = 2\Delta_{pg}$) and superconducting ($E_{sc} \sim 5k_B T_c$) energy scales, as a function of carrier doping x , is presented in figure 2 (only some representative datapoints are shown, so as not to overload the figure; similar compilations were also obtained by a number of other authors) [5, 9, 13, 16, 42, 43, 52, 57, 60, 70, 74, 75]. The data for these HTSCs with comparable $T_c^{\max} \sim 95$ K fall on two universal curves: a straight line for the pseudogap energy $E_{pg} = 2\Delta_{pg}$ and a parabola for the superconducting energy scale $E_{sc} \sim 5k_B T_c$. The two curves converge to the same $x \sim 0.27$ critical point at the end of the superconducting dome, similarly to the cartoon of figure 1(a). In order to summarize the situation with respect to quantitative estimates of E_{pg} and E_{sc} , we have listed in table 1 the values as determined by the different experimental techniques on optimally doped Bi2212 (with T_c ranging from 90 to 95 K). While one obtains from this compilation the average values of $E_{pg} \simeq 76$ meV and $E_{sc} \simeq 41$ meV at optimal doping, the numbers do scatter considerably. Note also that these numbers differ slightly from those given in relation

to the parabolic and straight lines in figure 2 (e.g. $E_{sc}^{\max} = 42$ meV) because the latter were inferred from a fitting of superconducting and pseudogap data over the whole doping range, while those in table 1 were deduced from results for optimally doped Bi2212 only. It is also possible to plot the pseudogap E_{pg} and superconducting E_{sc} energy scales as estimated simultaneously in one single experiment on the very same sample. This is done in figure 3 for Raman, tunneling and ARPES results from Bi2212 and Hg1201, which provide evidence for the presence of two energy scales, or possibly two spectral gaps as we discuss in greater detail below, coexisting over the whole superconducting dome.

2.1. Angle-resolved photoemission

The most extensive investigation of excitation gaps in HTSCs has arguably been done by ARPES [9, 10, 26, 27, 34, 35, 54–66, 76–80]. This technique provides direct access to the one-electron removal spectrum of the many-body system; it allows, for instance in the case of a BCS superconductor [29], to measure the momentum dependence of the absolute value of the pairing amplitude 2Δ via the excitation gap Δ observed for single-electron removal energies, again assuming E_F to be located half-way in the gap [9, 10]. This is the same in some tunneling experiments such as STM, which however do not provide direct momentum resolution but measure on both sides of E_F [18]. The gap magnitude is usually inferred from the ARPES spectra from along the normal-state Fermi surface in the antinodal region, where the d-wave gap is largest; it is estimated from the shift to high-binding energy of the quasiparticle spectral weight relative to the Fermi energy. With this approach only one gap is observed below a temperature scale that smoothly evolves from the so-called pseudogap temperature T^* in the underdoped regime, to the superconducting T_c on the overdoped side. We identify this gap

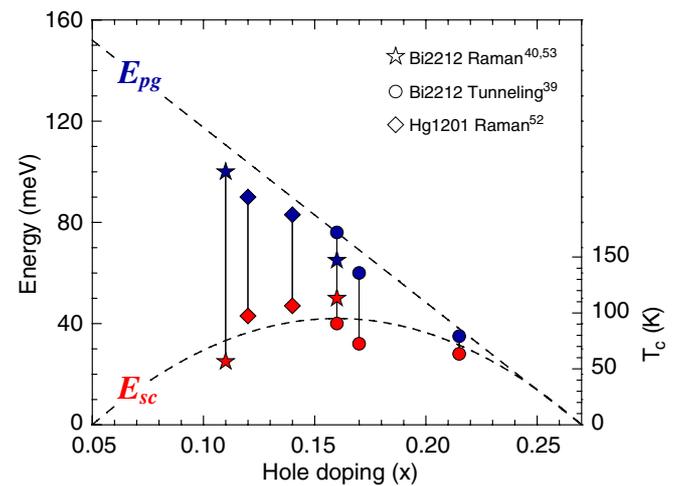


Figure 3. Pseudogap E_{pg} and superconducting E_{sc} energy scales (2Δ) as estimated, by a number of probes and for different compounds, in one single experiment on the very same sample. These data provide direct evidence for the simultaneous presence of two energy scales, possibly two spectral gaps, coexisting in the superconducting state. The superconducting and pseudogap lines are defined as in figure 2.

with the pseudogap energy scale $E_{pg} = 2\Delta_{pg}$. This is also in agreement with recent investigations of the near-nodal ARPES spectra from single and double layer Bi-cuprates [57, 76, 77], which further previous studies of the underdoped cuprates' Fermi arc phenomenology [78–80]. From the detailed momentum dependence of the excitation gap along the Fermi surface contour, and the different temperature trends observed in the nodal and antinodal regions, these studies suggest the coexistence of two distinct spectral gap components over the whole superconducting dome: superconducting gap and pseudogap, dominating the response in the nodal and antinodal regions, respectively, which would eventually collapse to one single energy scale in the very overdoped regime.

2.2. Tunneling

The HTSCs have been investigated by a wide variety of tunneling techniques [13, 18, 36–39, 44–51], such as SIN [38, 51], SIS [37–39], STM [18, 36, 46], intrinsic tunneling [47–50] and Andreev reflection, which is also a tunneling experiment but involves two-particle rather than single-particle tunneling (in principle, very much like SIS) [13, 43, 72]. All these techniques, with the exception of intrinsic tunneling³, are represented here either in the figures or table.

Similarly to what was discussed for ARPES at the antinodes, there are many STM studies that report a pseudogap E_{pg} smoothly evolving into E_{sc} upon overdoping [18, 31]. In addition, a very recent temperature-dependent study of overdoped single-layer Bi-cuprate detected two coexisting, yet clearly distinct, energy scales in a single STM experiment [32]. In particular, while the pseudogap was clearly discernible in the differential conductance exhibiting the usual large spatial modulation, the evidence for a spatially uniform superconducting gap was obtained by normalizing the low-temperature spectra by those just above $T_c \simeq 15$ K. These values have not been included in figures 2 and 3 because $T_c \ll 95$ K; however, this study arguably provides the most direct evidence for the coexistence of two distinct excitation gaps in the HTSCs.

One can regard Andreev reflection (pair creation in addition to a hole) as the inverse of a two-particle scattering experiment such as Raman or INS. A different view is also possible: SIN tunneling goes over to AR if the insulator layer gets thinner and thinner [13]; thus a SIN tunneling, as also STM, should give the same result as AR. However while SIN and STM measure the pseudogap, AR appears to be sensitive to the superconducting energy scale E_{sc} (figure 2). We can only conjecture that this has to do with the tunneling mechanisms actually being different.

³ The most convincing tunneling results showing two coexisting gaps were actually obtained by intrinsic tunneling [47–50], in particular from $\text{Bi}_2\text{Sr}_2\text{CuO}_{6+\delta}$ (Bi2201) [48]. However, because this technique suffers from systematic problems [50], and one would anyway have to scale the Bi2201 data because of the lower value of T_c and in turn gap energy scales, these results were not included in figures 2 or 3. Since intrinsic tunneling is in principle a clean SIS experiment which measures pair energies through Josephson tunneling, a refinement of the technique might provide an accurate estimate of both superconducting and pseudogap simultaneously, and is thus highly desirable.

SIS tunneling experiments [39] find $E_{pg}/E_{sc} \gtrsim 1$ for Bi2212 at all doping levels. There are, however, some open questions concerning the interpretation of the SIS experiments. This technique, which exploits Josephson tunneling, measures pair spectra; the magnitude of E_{pg} can readily be obtained from the most pronounced features in the spectra [39]. The signal related to E_{sc} is seen as a 'sideband' on the E_{pg} features; it does not seem obvious why, if the E_{sc} signal did originate from a state of paired electrons, it would not show up more explicitly.

2.3. Raman scattering

Light scattering measures a two-particle excitation spectrum providing direct insight into the total energy needed to break up a two-particle bound state or remove a pair from a condensate. Raman experiments can probe both superconducting and pseudogap energy scales, if one interprets the polarization dependent scattering intensity in terms of different momentum averages of the d-wave-like gap functions: one peaked at $(\pi, 0)$ in B_{1g} geometry, and thus more sensitive to the larger E_{pg} which dominates this region of momentum space; the other at $(\pi/2, \pi/2)$ in B_{2g} geometry, and provides an estimate of the slope of the gap function about the nodes, $(1/\hbar)(d\Delta/d\mathbf{k})|_n$, which is more sensitive to the arguably steeper functional dependence of E_{sc} out of the nodes [19, 40, 52, 53]. One should note, however, that the signal is often riding on a high background, which might result in a considerable error and data scattering. At a more fundamental level, while the experiments in the antinodal geometry allow a straightforward determination of the gap magnitude E_{pg} , the nodal results need a numerical analysis involving a normalization of the Raman response function over the whole Brillouin zone, a procedure based on a low-energy B_{2g} sum rule (although also the B_{2g} peak position leads to similar conclusions) [52]. This is because a B_{2g} Raman experiment is somewhat sensitive also to the gap in the antinodal direction, where it picks up, in particular, the contribution from the larger pseudogap.

2.4. Inelastic neutron scattering

Inelastic neutron scattering experiments have detected the so-called $q = (\pi, \pi)$ resonant magnetic mode in all of the $T_c \simeq 95$ K HTSCs considered here [16]. This resonance is proposed by some to be a truly collective magnetic mode that, much in the same way as phonons mediate superconductivity in the conventional BCS superconductors, might constitute the bosonic excitation mediating superconductivity in the HTSCs. The total measured intensity, however, amounts to only a small portion of what is expected based on the sum rule for the magnetic scattering from a spin 1/2 system [8, 16, 24, 42, 68, 69]; this weakness of the magnetic response should be part of the considerations in the modeling of magnetic resonance mediated high- T_c superconductivity. Alternatively, its detection below T_c might be a mere consequence of the onset of superconductivity and of the corresponding suppression of quasiparticle scattering. Independently of the precise interpretation, the INS data reproduced in figure 2 show that the magnetic resonance energy Ω_r tracks very closely, over the whole superconducting dome, the superconducting

energy scale $E_{sc} \sim 5k_B T_c$ (similar behavior is observed, in the underdoped regime, also for the spin-gap at the incommensurate momentum transfer $(\pi, \pi \pm \delta)$ [81]). Also remarkable is the correspondence between the energy of the magnetic resonance and that of the B_{2g} Raman peak. *Note that while the $q = (\pi, \pi)$ momentum transfer observed for the magnetic resonance in INS is a key ingredient of most proposed HTSC descriptions, Raman scattering is a $q = 0$ probe.* It seems that understanding the connection between Raman and INS might reveal very important clues.

2.5. Heat conductivity

Heat conductivity data from Y123 and Tl2201 fall onto the pseudogap line. This is a somewhat puzzling result because they have been measured at very low temperatures, well into the superconducting state, and should in principle provide a measure of both gaps together if these were indeed coexisting below T_c . However, similarly to the B_{2g} Raman scattering, these experiments are only sensitive to the slope of the gap function along the Fermi surface at the nodes, $(1/\hbar)(d\Delta/d\mathbf{k})_n$; the gap itself is determined through an extrapolation procedure in which only one gap was assumed. The fact that the gap values, especially for Y123, come out on the high side of the pseudogap line may be an indication that an analysis with two coexisting gaps might be more appropriate.

3. Outlook and conclusion

The data in figures 2 and 3 demonstrate that there are two coexisting energy scales in the HTSCs: one associated with the superconducting T_c and the other, as inferred primarily from the antinodal region properties, with the pseudogap T^* . The next most critical step is that of addressing the subtle questions concerning the nature of these energy scales and the significance of the emerging two-gap phenomenology towards the development of a microscopic description of high- T_c superconductivity.

As for the pseudogap, which grows upon underdoping, it seems natural to seek a connection to the physics of the insulating parent compound. Indeed, it has been pointed out that this higher energy scale might smoothly evolve, upon underdoping, into the quasiparticle dispersion observed by ARPES in the undoped antiferromagnetic insulator [82, 83]. At zero doping the dispersion and quasiparticle weight in the single-hole spectral function as seen by ARPES can be very well explained in terms of a self-consistent Born approximation [84], as well as in the diagrammatic quantum Monte Carlo [85] solution to the so-called $t-t'-t''-J$ model. In this model, as in the experiment [82, 83], the energy difference between the top of the valence band at $(\pi/2, \pi/2)$ and the antinodal region at $(\pi, 0)$ is a gap due to the quasiparticle dispersion of about 250 ± 30 meV. Note that this would be a single-particle gap Δ . For the direct comparison with the pseudogap data in figure 2, we would have to consider $2\Delta \sim 500$ meV; this, however, is much larger than the $x = 0$ extrapolated pseudogap value of 186 meV found from our analysis across the phase diagram. Thus there seems to be an

important disconnection between the finite doping pseudogap and the zero-doping quasiparticle dispersion.

The fact that the pseudogap measured in ARPES and SIN experiments is only half the size of the gap in SIS, STM, B_{1g} Raman and heat conductivity measurements, points to a pairing gap. So although the origin of the pseudogap at finite doping remains uncertain, we are of the opinion that it most likely reflects a pairing energy of some sort. To this end, the trend in figure 2 brings additional support to the picture discussed by many authors that the reduction in the density of states at T^* is associated with the formation of electron pairs, well above the onset of phase coherence taking place at T_c (see, e.g. [86, 87]). The pseudogap energy $E_{pg} = 2\Delta_{pg}$ would then be the energy needed to break up a preformed pair. To conclusively address this point, it would be important to study very carefully the temperature dependence of the $(\pi, 0)$ response below T_c ; any further change with the onset of superconductivity, i.e. an increase in E_{pg} , would confirm the two-particle pairing picture, while a lack thereof would suggest a one-particle band structure effect as a more likely interpretation of the pseudogap.

The lower energy scale connected to the superconducting T_c (parabolic curve in figure 2 and 3) has already been proposed by many authors to be associated with the condensation energy [86–89], as well as with the magnetic resonance in INS [90]. One might think of it as the energy needed to take a pair of electrons out of the condensate; however, for a condensate of charged bosons, a description in terms of a collective excitation, such as a plasmon or roton, would be more appropriate [24]. The collective excitation energy would then be related to the superfluid density and in turn to T_c . In this sense, this excitation would truly be a two-particle process and should not be measurable by single-particle spectroscopies. Also, if the present interpretation is correct, this excitation would probe predominantly the charge-response of the system; however, there must be a coupling to the spin channel, so as to make this process neutron active (yet not as intense as predicted by the sum rule for pure spin-1/2 magnetic excitations, which is consistent with the small spectral weight observed by INS). As discussed, one aspect that needs to be addressed to validate these conjectures is the surprising correspondence between $q = 0$ and $q = (\pi, \pi)$ excitations, as probed by Raman and INS, respectively.

We are led to the conclusion that the coexistence of two energy scales is essential for high- T_c superconductivity, with the pseudogap reflecting the pairing strength and the other, always smaller than the pseudogap, the superconducting condensation energy. This supports the proposals that the HTSCs cannot be considered as classical BCS superconductors, but rather are smoothly evolving from the BEC into the BCS regime [91–93], as carrier doping is increased from the underdoped to the overdoped side of the phase diagram.

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References

- [1] Bednorz J G and Müller K A 1986 Possible high- T_c superconductivity in the Ba-La-Cu-O system *Z. Phys. B* **64** 189–93
- [2] Pickett W E 1989 Electronic structure of the high-temperature oxide superconductors *Rev. Mod. Phys.* **61** 433–512
- [3] Dagotto E 1994 Correlated electrons in high-temperature superconductors *Rev. Mod. Phys.* **66** 763–841
- [4] Kastner M A, Birgeneau R J, Shirane G and Endoh Y 1998 Magnetic, transport, and optical properties of monolayer copper oxides *Rev. Mod. Phys.* **70** 897–928
- [5] Timusk T and Statt B W 1999 The pseudogap in high-temperature superconductors: an experimental survey *Rep. Prog. Phys.* **62** 61–122
- [6] Orenstein J and Millis A J 2000 Advances in the physics of high-temperature superconductivity *Science* **288** 468–74
- [7] Tsui C C and Kirtley J R 2000 Pairing symmetry in cuprate superconductors *Rev. Mod. Phys.* **72** 969–1016
- [8] Norman M R and Pepin C 2003 The electronic nature of high temperature cuprate superconductors *Rep. Prog. Phys.* **66** 1547–610
- [9] Damascelli A, Hussain Z and Shen Z-X 2003 Angle-resolved photoemission studies of the cuprate superconductors *Rev. Mod. Phys.* **75** 473–541
- [10] Campuzano J C, Norman M R and Randeria M 2004 *Photoemission in the High T_c Superconductors* vol 2 (Berlin: Springer) pp 167–265
- [11] Chen Q, Stajic J, Tan S and Levin K 2005 BCS-BEC crossover: from high temperature superconductors to ultracold superfluids *Phys. Rep.* **412** 1–88
- [12] Norman M R, Pines D and Kallin C 2005 The pseudogap: friend or foe of high T_c ? *Adv. Phys.* **54** 715–33
- [13] Deutscher G 2005 Andreev–Saint-James reflections: a probe of cuprate superconductors *Rev. Mod. Phys.* **77** 109–35
- [14] 2006 Special issue on high-temperature superconductors *Nat. Phys.* **2** 133–210
- [15] Millis A J 2006 Gaps and our understanding *Science* **314** 1888–9
- [16] Eschrig M 2006 The effect of collective spin-1 excitations on electronic spectra in high- T_c superconductors *Adv. Phys.* **55** 47–183
- [17] Cho A 2006 High T_c : the mystery that defies solution *Science* **314** 1072–5
- [18] Fischer Ø, Kugler M, Maggio-Aprile I, Berthod C and Renner C 2007 Scanning tunneling spectroscopy of high-temperature superconductors *Rev. Mod. Phys.* **79** 353–419
- [19] Devereaux T P and Hackl R 2007 Inelastic light scattering from correlated electrons *Rev. Mod. Phys.* **79** 175–233
- [20] Schrieffer J R (ed) 2007 *Treatise of High Temperature Superconductivity* (Berlin: Springer)
- [21] Lee P A, Nagaosa N and Wen X-G 2007 Doping a Mott insulator: physics of high-temperature superconductivity *Rev. Mod. Phys.* **78** 17–85
- [22] Basov D N and Timusk T 2005 Electrodynamics of high- T_c superconductors *Rev. Mod. Phys.* **77** 721–79
- [23] Leggett A J 2006 What do we know about high T_c ? *Nat. Phys.* **2** 134–6
- [24] Uemura Y J 2006 Twin spin/charge roton mode and superfluid density: primary determining factors of T_c in high- T_c superconductors observed by neutron, ARPES, and μ SR *Physica B* **374** 1–8
- [25] Batlogg B, Hwang H Y, Takagi H, Cava R J, Kao H L and Kwo J 1994 Normal state phase diagram of $(\text{La,Sr})_2\text{CuO}_4$ from charge and spin dynamics *Physica C* **130** 235–40
- [26] Loeser A G, Shen Z-X, Dessau D S, Marshall D S, Park C H, Fournier P and Kapitulnik A 1996 Excitation gap in the normal state of underdoped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ *Science* **273** 325–9
- [27] Ding H, Yokoya T, Campuzano J C, Takahashi T, Randeria M, Norman M R, Mochiku T, Hadowaki K and Giapintzakis J 1996 Spectroscopic evidence for a pseudogap in the normal state of underdoped high- T_c superconductors *Nature* **382** 51–4
- [28] Tsuei C C and Kirtley J R 2000 Pairing symmetry in cuprate superconductors *Rev. Mod. Phys.* **72** 969–1016
- [29] Bardeen J, Cooper L N and Schrieffer J R 1957 Theory of superconductivity *Phys. Rev.* **108** 1175–204
- [30] Goss Levi B 2007 New experiments fuel debate over the nature of high- T_c superconductors *Phys. Today* **60** 17–21
- [31] Gomes K K, Pasupathy A N, Pushp A, Ono S, Ando Y and Yazdani A 2007 Visualizing pair formation on the atomic scale in the high- T_c superconductor $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+y}$ *Nature* **447** 569–72
- [32] Boyer M C, Wise W D, Chatterjee K, Yi M, Kondo K, Takeuchi T, Ikuta H and Hudson E W 2007 Imaging the two gaps of the high-temperature superconductor $\text{Bi}_2\text{Sr}_2\text{CuO}_{6+x}$ *Nat. Phys.* **3** 802–6
- [33] Kohsaka Y *et al* 2007 An intrinsic bond-centered electronic glass with unidirectional domains in underdoped cuprates *Science* **315** 1380–5
- [34] Fedorov A V, Valla T, Johnson P D, Li Q, Gu G D and Koshizuka N 1999 Temperature dependent photoemission studies of optimally doped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ *Phys. Rev. Lett.* **82** 2179–82
- [35] Ding H, Engelbrecht J R, Wang Z, Campuzano J C, Wang S-C, Yang H-B, Rogan R, Takahashi T, Kadowaki K and Hinks D G 2001 Coherent quasiparticle weight and its connection to high- T_c superconductivity from angle-resolved photoemission *Phys. Rev. Lett.* **87** 227001
- [36] McElroy K, Lee D-H, Hoffman J E, Lang K M, Lee J, Hudson E W, Eisaki H, Uchida S and Davis J C 2005 Coincidence of checkerboard charge order and antinodal state decoherence in strongly underdoped superconducting $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ *Phys. Rev. Lett.* **94** 197005
- [37] Miyakawa N, Guptasarma P, Zasadzinski J F, Hinks D G and Gray K E 1998 Strong dependence of the superconducting gap on oxygen doping from tunneling measurements on $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8-\delta}$ *Phys. Rev. Lett.* **80** 157–60
- [38] Miyakawa N, Zasadzinski J F, Ozyuzer L, Guptasarma P, Hinks D G, Kendziora C and Gray K E 1999 Predominantly superconducting origin of large energy gaps in underdoped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ from tunneling spectroscopy *Phys. Rev. Lett.* **83** 1018–21
- [39] Zasadzinski J F, Ozyuzer L, Miyakawa N, Gray K E, Hinks D G and Kendziora C 2001 Correlation of tunneling spectra in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ with the resonance spin excitation *Phys. Rev. Lett.* **87** 067005

- [40] Venturini F, Opel M, Hackl R, Berger H, Forro L and Revaz B 2002 Doping dependence of the electronic Raman spectra in cuprates *J. Phys. Chem. Solids* **63** 2345–8
- [41] Puchkov A V, Basov D N and Timusk T 1996 The pseudogap state in high- T_c superconductors: an infrared study *J. Phys.: Condens. Matter* **8** 10049–82
- [42] Sidis Y, Pailhes S, Keimer B, Bourges P, Ulrich C and Regnault L P 2004 Magnetic resonant excitations in high- T_c superconductors *Phys. Status Solidi B* **241** 1204–10
- [43] Deutscher G 1999 Coherence and single-particle excitations in the high-temperature superconductors *Nature* **397** 410–2
- [44] Shibauchi T, Krusin-Elbaum L, Li M, Maley M P and Kes P H 2001 Closing the pseudogap by Zeeman splitting in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+y}$ at high magnetic fields *Phys. Rev. Lett.* **86** 5763–6
- [45] Krusin-Elbaum L, Shibauchi T, Blatter G, Mielke C H, Li M, Maley M P and Kes P H 2003 Pseudogap state in overdoped $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+y}$ *Physica C* **387** 169–74
- [46] Lee J *et al* 2006 Interplay of electron-lattice interactions and superconductivity in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ *Nature* **442** 546–50
- [47] Krasnov V M, Yurgens A, Winkler D, Delsing P and Claeson T 2000 Evidence for coexistence of the superconducting gap and the pseudogap in Bi-2212 from intrinsic tunneling spectroscopy *Phys. Rev. Lett.* **84** 5860–3
- [48] Yurgens A, Winkler D, Claeson T, Ono S and Ando Y 2003 Intrinsic tunneling spectra of $\text{Bi}_2(\text{Sr}_{2-x}\text{La}_x)\text{CuO}_{6+\delta}$ *Phys. Rev. Lett.* **90** 147005
- [49] Suzuki M and Watanabe T 2000 Discriminating the superconducting gap from the pseudogap in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ by interlayer tunneling spectroscopy *Phys. Rev. Lett.* **85** 4787–90
- [50] Zhao S P, Zhu X B and Wei Y F 2007 Intrinsic tunneling spectra of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ near optimal doping *Preprint cond-mat/0703177*
- [51] Zasadzinski J F, Ozyuzer L, Coffey L, Gray K, Hinks D G and Kendziora C 2003 Intrinsic tunneling spectra of $\text{Bi}_2(\text{Sr}_{2-x}\text{La}_x)\text{CuO}_{6+\delta}$ *Phys. Rev. Lett.* **90** 147005
- [52] Le Tacon M, Sacuto A, Georges A, Kotliar G, Gallais Y, Colson D and Forget A 2006 Two energy scales and two distinct quasiparticle dynamics in the superconducting state of underdoped cuprates *Nat. Phys.* **2** 537–43
- [53] Sugai S, Suzuki H, Takayanagi Y, Hosokawa T and Hayamizu N 2003 Carrier-density-dependent momentum shift of the coherent peak and the LO phonon mode in p-type high- T_c superconductors *Phys. Rev. B* **68** 184504
- [54] Mesot J *et al* 1999 Superconducting gap anisotropy and quasiparticle interactions: a doping dependent photoemission study *Phys. Rev. Lett.* **83** 840–3
- [55] Kondo T, Takeuchi T, Kaminski A, Tsuda S and Shin S 2007 Evidence for two energy scales in the superconducting state of optimally doped $(\text{Bi,Pb})_2(\text{Sr,L a})_2\text{CuO}_{6+\delta}$ *Phys. Rev. Lett.* **98** 267004
- [56] Yoshida T *et al* 2007 Low-energy electronic structure of the high- T_c cuprates $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ studied by angle-resolved photoemission spectroscopy *J. Phys.: Condens. Matter* **19** 125209
- [57] Tanaka K *et al* 2006 Distinct Fermi-momentum-dependent energy gaps in deeply underdoped Bi2212 *Science* **314** 1910–3
- [58] Valla T, Fedorov A V, Lee J, Davis J C and Gu G D 2006 The ground state of the pseudogap in cuprate superconductors *Science* **314** 1914–6
- [59] Platé M *et al* 2005 Fermi surface and quasiparticle excitations of overdoped Tl2201 by ARPES *Phys. Rev. Lett.* **95** 077001
- [60] Peets D C, Mottershead J D F, Wu B, Elfimov I S, Liang R, Hardy W N, Bonn D A, Raudsepp M, Ingle N J C and Damascelli A 2007 $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ brings spectroscopic probes deep into the overdoped regime of the high- T_c cuprates *New J. Phys.* **9** 28
- [61] Gromko A D, Fedorov A V, Chuang Y-D, Koralek J D, Aiura Y, Yamaguchi Y, Oka K, Ando Y and Dessau D S 2003 Mass-renormalized electronic excitations at $(\pi, 0)$ in the superconducting state of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ *Phys. Rev. B* **68** 174520
- [62] Cuk T, Baumberger F, Lu D H, Ingle N, Zhou X J, Eisaki H, Kaneko N, Hussain Z, Devereaux T P, Nagaosa N and Shen Z-X 2004 Coupling of the B_{1g} phonon to the antinodal electronic states of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_8$ *Phys. Rev. Lett.* **93** 117003
- [63] Fink J, Koitzsch A, Geck J, Zabolotny V, Knupfer M, Buchner B, Chubukov A and Berger H 2006 Reevaluation of the coupling to a bosonic mode of the charge carriers in $(\text{Bi,Pb})_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ at the antinodal point *Phys. Rev. B* **74** 165102
- [64] Campuzano J C *et al* 1999 Electronic spectra and their relation to the (π, π) collective mode in high- T_c superconductors *Phys. Rev. Lett.* **83** 3709–12
- [65] Johnson P D *et al* 2001 Doping and temperature dependence of the mass enhancement observed in the cuprate $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ *Phys. Rev. Lett.* **87** 177007
- [66] Kordyuk A A and Bosisenko S V 2006 ARPES on high-temperature superconductors: simplicity vs. complexity *Low Temp. Phys.* **32** 298–304
- [67] Dordevic S V, Homes C C, Tu J J, Valla T, Strongin M, Johnson P D, Gu G D and Basov D N 2005 Extracting the electron-boson spectral function $\alpha^2 F(\omega)$ from infrared and photoemission data using inverse theory *Phys. Rev. B* **71** 104529
- [68] Dai P, Mook H A, Hunt R D and Dogan F 2001 Evolution of the resonance and incommensurate spin fluctuations in superconducting $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ *Phys. Rev. B* **63** 054525
- [69] He H, Bourges P, Sidis Y, Ulrich C, Regnault L P, Pailhes S, Berzigiarova N S, Kolesnikov N N and Keimer B 2002 Magnetic resonant mode in the single-layer high-temperature superconductor $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ *Science* **295** 1045–7
- [70] Sutherland M *et al* 2003 Thermal conductivity across the phase diagram of cuprates: low-energy quasiparticles and doping dependence of the superconducting gap *Phys. Rev. B* **67** 174520
- [71] Hawthorn D G *et al* 2007 Doping dependence of the superconducting gap in $\text{Tl}_2\text{Ba}_2\text{CuO}_{6+\delta}$ from heat transport *Phys. Rev. B* **75** 104518
- [72] Deutscher G 1999 Superconducting gap and pseudogap *Low Temp. Phys.* **397** 410–2
- [73] Eisaki H, Kaneko N, Feng D L, Damascelli A, Mang P K, Shen K M, Shen Z-X and Geven M 2004 Effect of chemical inhomogeneity in bismuth-based copper oxide superconductors *Phys. Rev. B* **69** 064512
- [74] Panagopoulos C and Xiang T 1998 Relationship between the superconducting energy gap and the critical temperature in high- T_c superconductors *Phys. Rev. Lett.* **81** 2336
- [75] Valenzuela B and Bascones E 2007 Phenomenological description of the two energy scales in underdoped cuprate superconductors *Phys. Rev. Lett.* **98** 227002
- [76] Kondo T, Takeuchi T, Kaminski A, Tsuda S and Shin S 2007 Evidence for two energy scales in the superconducting state of optimally doped $(\text{Bi,Pb})_2(\text{Sr,L a})_2\text{CuO}_{6+\delta}$ *Phys. Rev. Lett.* **98** 267004
- [77] Lee W S, Vishik I M, Tanaka K, Lu D H, Sasagawa T, Nagaosa N, Devereaux T P, Hussain Z and Shen Z-X 2007 Abrupt onset of a second energy gap at the superconducting transition of underdoped Bi2212 *Nature* **450** 81–4
- [78] Norman M R *et al* 1998 Destruction of the Fermi surface in underdoped high- T_c superconductors *Nature* **392** 157–60

- [79] Kanigel A *et al* 2006 Evolution of the pseudogap from Fermi arcs to the nodal liquid *Nat. Phys.* **2** 447–51
- [80] Shen K M *et al* 2005 Nodal quasiparticles and antinodal charge ordering in $\text{Ca}_{2-x}\text{Na}_x\text{CuO}_2\text{Cl}_2$ *Science* **307** 901–4
- [81] Chang J *et al* 2007 Magnetic-field-induced spin excitations and renormalized spin gap of the underdoped $\text{La}_{1.895}\text{Sr}_{0.105}\text{CuO}_4$ superconductor *Phys. Rev. Lett.* **98** 077004
- [82] Ronning F, Kim C, Feng D L, Marshall D S, Loeser A G, Miller L L, Eckstein J N, Bozovic L and Shen Z-X 1998 Photoemission evidence for a remnant Fermi surface and a d-wave-like dispersion in insulating $\text{Ca}_2\text{CuO}_2\text{Cl}_2$ *Science* **282** 2067–72
- [83] Ronning F *et al* 2003 Universality of the electronic structure from a half-filled CuO_2 Plane *Phys. Rev. B* **67** 035113
- [84] Sushkov O P, Sawatzky G A, Eder R and Eskes H 1997 Hole photoproduction in insulating copper oxide *Phys. Rev. B* **56** 11769
- [85] Prokof'ev N V and Svistunov B V 1998 Polaron problem by diagrammatic quantum Monte Carlo *Phys. Rev. Lett.* **81** 2514–7
- [86] Kotliar G 1988 Resonating valence bonds and d-wave superconductivity *Phys. Rev. B* **37** 3664–6
- [87] Emery V J and Kivelson S A 1995 Importance of phase fluctuations in superconductors with small superfluid density *Nature* **374** 434–7
- [88] Kotliar G and Liu J 1988 Superexchange mechanism and d-wave superconductivity *Phys. Rev. B* **38** 5142–5
- [89] Uemura Y J *et al* 1989 Universal correlations between T_c and n_s/m^* (carrier density over effective mass) in high- T_c cuprate superconductors *Phys. Rev. Lett.* **62** 2317–20
- [90] Zhang S-C 1997 A unified theory based on $SO(5)$ symmetry of superconductivity and antiferromagnetism *Science* **275** 1089–96
- [91] Leggett A J 2006 *Quantum Liquids* (Oxford: Oxford University Press)
- [92] Leggett A J 1980 *Modern Trends in the Theory of Condensed Matter* (Berlin: Springer) pp 13–27
- [93] Nozieres P and Schmitt-Rink S 1985 Bose condensation in an attractive fermion gas: from weak to strong coupling superconductivity *J. Low Temp. Phys.* **59** 195–211